

Topics for Test #2, MA242

1. Be able to compute first and second partial derivatives.
2. Be able to compute directional derivatives.
3. Be able to prove whether or not a multivariable function is **continuous** at a point.
4. Be able to prove whether or not a multivariable function is **differentiable** at a point.
5. Be able to use the chain rule to compute partial derivatives of composite functions.
6. Be able to find equation of:
  - (a) the tangent plane to the graph  $z = f(x, y)$  of a function of two variables
  - (b) the tangent plane to the  $c$ -level surface  $f(x, y, z) = c$  of a function of three variables
7. Know how to compute the gradient of a multivariable function.
8. Know what information the gradient of a function tells you about a given multivariable function.
9. Know how to find the linear approximation of a multivariable function near a point.
10. Know how to find the critical points of a function  $f(x, y)$ , and be able to use the second derivative test to determine if each critical point corresponds to a local maximum, local minimum or saddle point.
11. Know how to determine the global maximum and minimum values of a **continuous** function  $f(x, y)$  on a closed and bounded region  $D \subset \mathbb{R}^2$ .